Optical study of atomic monolayers

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Introduction

Graphene monolayer

Novoselov, Geim et al. prepared graphitic sheets of thickness down to a few atomic layers, including a single layer graphene, to fabricate devices and to study their electronic properties. [Novoselov et al., Science, **306**, 666 (2004)]

Fig. 1. Graphene films. (A) Photograph (in normal white light) of a relatively large multilayer graphene flake with thickness ~3 nm on top of an oxidized Si wafer. (B) Atomic force microscope (AFM) image of 2 um by 2 um area of this flake near its edge. Colors: dark brown, SiO, surface; orange, 3 nm height above the SiO₂ surface. (C) AFM image of single-layer graphene. Colors: dark brown, SiO, surface; brown-red (central area), 0.8 nm height; yellow-brown (bottom left), 1.2 nm; orange (top left), 2.5 nm. Notice the folded part of the film near the bottom, which exhibits a differential height of ~0.4 nm. For details of AFM imaging of single-layer graphene, see (15). (D) Scanning electron microscope image of one of our experimental devices prepared from FLG. (E) Schematic view of the device in (D).

Atomic monolayer (ML) structures

- The discovery of the synthesis of graphene sheets stimulated the studies of other materiales arranged in atomic MLs, e.g. BN, silicene, germanene, transition metal dichalcogenade structures, phosphorene, etc.
- Two dimensional 2D structures consist of a certain number of crystalline layers.
- The physical properties of atomic ML structures differ very significantly to those of the respective bulk structures.
- Wide applications: electronic and photovoltaic devices, sensors, spintronics, etc
- Our interes focuses in the optical studies of atomic ML structures, through the calculation of their lineal, non linear and spin injection response.

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Method

- Quantum Method First principles
- Density Functional Theory (DFT) LDA (GGA) Approximation
- GW method to obtain quasiparticle energies

Note: The [ABINIT](http://www.cio.mx) code has been used.

Steps for the calculation of the optical response

- Calculation of the lattice constant and atomic positions.
- Calculation of the wave functions and LDA energy states.
- Calculation of the GW energies.
- Calculation of the momentum and spin matrix elements.
- Calculation of the optical response (linear, nonlinear, spin injection).

First order optical response

Dielectric function

 $\varepsilon(\omega) = \varepsilon_1(\omega) + i \varepsilon_2(\omega)$

where the imaginary part is given by:

$$
\epsilon_2^{ab}(\omega) = 4\pi \Im \mathfrak{m} \chi_1^{ab}(-\omega; \omega)
$$

$$
\epsilon_2^{ab}(\omega) = \frac{4\pi^2 e^2}{\hbar} \int \frac{d\mathbf{k}}{8\pi^3} \sum_{nm} f_{nm} r_{nm}^a r_{mn}^b \delta(\omega_{mn} - \omega)
$$

r_{*mn*} are the position matrix elements,

 $\omega_{mn} = \omega_m - \omega_n$ are the transition frequencies between states *m* and *n*, **k** the wavevector,

 $f_{nm} = f_n - f_m$; and the Fermi factor $f_n = (1, 0)$, for (valence, conduction) bands. [J.E. Sipe and A.I. Shkrebtii, PRB **61**, 5337 (2000)]

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Layered In₂Se₃ structures

- • Indium Selenide In₂Se₃ layered structures have attracted attention.
- Due to its polymorphism, In₂Se₃ have different phases α , β , γ .
- \bullet The α phase has the lowest energy and belongs to the R3m space group.
- The layered estructure consists of 5 atomic layers
- \bullet Ding et al. demostrated the ferroelectric nature of In₂Se₃ QL [Ding et al., Nature Comm. **8**, 14956 (2017)].
- Zhou et al. reported the first experimental evidence of the out-of-plane ferroelectricity for the layered α -In₂Se₃ structure. [Y. Zhou et al. Nano Letters, **17**, 5508 (2017)]
- Ding et al. theoretically found two possible stable atomic configurations within 1QL: the wurtzite and zincblende type denoted by FE-ZB' and FE-WZ'.
- Applications: memory devices, thin films ferroelectrics, sensors, etc.

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α*-*In2Se³ structures

FE-ZB' - 1QL Unit cell $a=4.106$ Å

Top and side views

FE-WZ' - 1QL $a=4.106$ Å

Dielectric function $\varepsilon_2(\hbar\omega)$

Ferroelectric nature of In₂Se₃

Ding et al. demostrated the ferroelectric nature of In_2Se_3 QL as a result of the lost of centrosymmetry of the middle Se atom. It presents both out-of-plane and in-plane electric polarization. [Ding et al., Nature Comm. **8**, 14956 (2017)].

Parameter values: psp: HGH; *E^c* =40 Ha Vaccuum lenght = 2c $\frac{1}{2}$ For 1 ML: $E_g^{LDA} =$ 0.62 eV; $E_g^{LDA-sc} =$ 0.58 eV; $E_g^{GGA} =$ 0.79 eV (Ding); $E_g^{\text{exp}} = 1.3 \text{ eV}$ [ACS Nano, **8**, 514 (2014)]; For 2ML (net \vec{p}): There is no band gap in LDA; For 2ML ($\vec{\rho} = 0$): E_g^{LDA} =0.46 eV. (indirect); E_g^{LDA} =0.75 eV. (direct);

Dielectric function $\varepsilon_2(\hbar\omega)$ FE-WZ' 2QL structure with $\vec{p} = 0$

Parameter values:

psp: HGH; $E_c = 40$ Ha nkpt=324 (IBZ) Vaccuum lenght = 2c

For 1 ML: E_g^{LDA} =0.62 eV; *E exp* $=1.3$ eV $[ACS$ Nano, **8**, 514 (2014)];

For 2ML ($\vec{p} = 0$): E_g^{LDA} =0.46 eV. (I); E_g^{LDA} =0.75 eV. (D);

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Total energy Vs stacking point $FE-WZ' - In₂Se₃ 2QL, $\vec{p} = 0$$

Dielectric function and Transmission

For the α -In₂Se₃ structure.

- Different dielectric function curves are generated by averaging over the various stacking arrangements.
- Different transmission curves with the same color correspond to the \bullet various stacking arrangements.

Second order response $|\chi^{(\mathsf{2})}|$

 α -In₂Se₃ structure belongs to the R3m symmetry group and has four independent non-vanishing components of the NL susceptibility: zzz , $zxx = zyy$, $xxz = yyz$, $xxx = xyy = yyx$

The second order NL susceptibility is sensitive to changes to the atomic structure.

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Summary

We have studied the linear and non linear optical response of α -In₂Se₃ structure

Conclusions

- The linear response is sensitive to the number of QLs or thicknesses of the structure.
- The transmission spectra in overall decrese as the number of QLs increase.
- The nonlinear optical response is more sensitive to changes in the atomic structure.

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*MoS*² *monolayer structure*

ATOMIC STRUCTURE: 2H-MoS₂, hexagonal, ABAB stacking FAMILY: Transition-metal dichalcogenides SPATIAL GROUP FOR THE BULK STRUCTURE: $P63/mmc$ SPATIAL GROUP FOR THE MONOLAYER STRUCTURE: P6m2

Characteristics of the MoS₂ structures

• The bulk structure of $MoS₂$ is centrosymmetric (CS).

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- Monolayer structures of $MoS₂$ with an even number of layers are CS.
- Monolayer structures of MoS₂ with an odd number of layers are non CS.

- Lattice constant (exp): $a = 3.16$ Å, $c = 12.296$ Å.
- Calculus of the wave functions and eigenenergies using DFT-LDA with the help of abinit.
- Relativistic pseudopotentials (HGH). *v e* (*s* and *p*) for S; and 6 *v e* (*s* and *d*) for Mo.
- GW Correction of the LDA band gap energy at Γ.
- The ML structure was modeled as a supercell.

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Spin injection in semiconductors

- Spin-polarized electrons can be generated in the conduction bands of nonmagnetic semiconductors τ*^e* (ps-ns)>> τ*^h* (fs).
	- Electrical injection. J. Phys. Condens. Matter, **28** 453003 (2016)
	- Optical injection: by one or two-photon absorption of circularly polarized light.

PRB, **71**, 035209 (2005), PRL **90**, 216601 (2003).

Optical spin injection

The optical spin generation is based on:

- The absorption of circularly polarized light.
- Optical selection rules.
- The spin-orbit (SO) interaction.

In the process of spin injection, there is an interference between two coherent spin states, whose energy difference is ∆*E* ≈ meV

*Degree of spin polarization (*DSP*)*

$$
\text{DSP} = \frac{N_{\downarrow} - N_{\uparrow}}{N_{\downarrow} + N_{\uparrow}}
$$

 N_{\perp} (N_{\uparrow}) is the density of spin-down (-up) polarized electrons. Experiment: Polarization resolved pump probe experiment in GaAs.

- Bath et al. calculated DSP as a function of excess energy for GaAs, InP, GaSb, InSb, y ZnSe.
- These materials present 50% of DSP just at the band gap energy for onephoton excitation.

Theory

The DSP in the direction *a* is given by

$$
\mathcal{D}^\mathsf{a}(\ell,\omega)=\frac{\dot{\mathcal{S}}^\mathsf{a}(\ell,\omega)}{(\hbar/2)\dot{n}(\ell,\omega)}.
$$

The incident optical electric field is circularly polarized

 $\mathsf{E}(\omega) = \mathsf{E}_0(\omega)(\hat{x} + i\hat{y})/$ √ 2.

Spin generation rate

$$
\dot{S}^{\rm a}(\ell;\omega)=\zeta^{\rm abc}(\ell;\omega)E^{\rm b}(-\omega)E^{\rm c}(\omega)
$$

Rate of generation of charge carriers

$$
\dot{\eta}(\ell;\omega)=\xi^{\rm ab}(\ell;\omega)E^{\rm a}(-\omega)E^{\rm b}(\omega)
$$

$$
\zeta^{abc}(\ell,\omega) = \frac{\pi e^2}{\hbar^2} \int \frac{d\mathbf{k}}{8\pi^3} \sum_{cc'v} S^a_{c'c}(\ell,\mathbf{k}) r^b_{vc'}(\mathbf{k}) r^c_{cv}(\mathbf{k})
$$

$$
\times \left[\delta(\omega - \omega_{cv}(\mathbf{k})) + \delta(\omega - \omega_{c'v}(\mathbf{k})) \right] \tag{1}
$$

$$
\xi^{ab}(\ell;\omega) = \frac{\pi e^2}{\hbar^2} \int \frac{d\mathbf{k}}{8\pi^3} \sum_{\text{vcc}'}' \text{Re}\big[\varrho_{c'c}(\ell; \mathbf{k}) r_{\text{vc}}^a(\mathbf{k}) r_{\text{cv}}^b(\mathbf{k})\n+ \varrho_{\text{cc}'}(\ell; \mathbf{k}) r_{\text{vc}}^a(\mathbf{k}) r_{\text{cv}}^b(\mathbf{k})\big] \delta(\omega_{\text{cv}}(\mathbf{k}) - \omega) \qquad (2)
$$
\nc and c' are causal
generate conduction bands (~ 30 meV)

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Results

DSP in bulk GaAs

Experiment

Bhat et al., PRB **71** (2005)

K and **K**['] have opposite sign in the DSP, which is ruled by the time reversal symmetry

$$
E(\textbf{k},\uparrow)=E(-\textbf{k},\downarrow)
$$

- Chang et al. considered that DSP is equal to zero in ML structures with an even number of layers since they are CS. Chang et al., Scientific Reports **4**, 6270 (2014).
- For ML structures with an odd number of layers N, they considered that DSP varied as 1/N.

Dresselhaus effect

G. Dresselhaus et al., Phys. Review **100**, 580 (1955).

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- Dresselhaus estudied the SO effects in zincblende crystals (GaAs, InSb, CdTe).
- The SOC generates a field **B***eff* ∼ [∇*V*(**r**) × **p**)], which leads to the spin-splitting of the bands and spin polarization.
- He reported an anisotropic spin splitting of the bands in non CS systems.

Rashba effect

- E.I. Rashba and V.I. Sheka, Fiz. Tverd. Tela: Collected papers **2**, 162-76 (1959).
- G. Bihlmayer et al., New J. Phys. **17**, 050202 (2015).
	- Rashba and Sheka reported that the spin splitting of the bands of wurtzite hexagonal systems corresponding to *s* electrons at around Γ is linear and isotropic in the wave vector **k** perpendicular to the *c* axis.

Spin polarization in CS systems

Considering the Dresselhaus and Rashba effects, it is expected that a 3D material does not have inversion symmetry in order to present spin splitting, and thus spin polarization

Compensated spin polarization

X. Zhang. et al. Nature Physics, **10**, 387 (2014).

- Zhang et al. showed that the local symmetry of the system determine the SO interaction
- They reported that, in CS media, though all bands are degenerated, there are two components of the degenerated bands that can have opposite spin polarization corresponding to sectors of the system that mutually present inversion.
- Compensated spin polarization can occur in CS systems with spatial groups $P6_3/mmc$ (e.g. MoS₂), $R\overline{3}m$ y $P4/nmm$.

DSP *- MoS*2*-ML Arzate et al., PRB* **⁹³***, 115433 (2016).*

- Calculus of DSP in the whole BZ.
- Convergence with 2912 (392) **k** points in the IBZ in MoS₂ ML (bulk) structures.
- Cut off energy of 40 Ha.

$DSP - MoS_2-ML$

Arzate et al., PRB **93**, 115433 (2016).

Spin generation - MoS₂-ML

Arzate et al., PRB **93**, 115433 (2016).

DSP *- Comparison*

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Summary

We have teoretically studied the optical response and spin injection of atomic monolayer of $MoS₂$ structures

Conclusions

- It is possible to inject spin-polarized electrons into the conduction bands of molybdenum disulfide monolayer structures with circularly polarized light.
- The DSP of the MoS₂ ML is of 100% at the photon energy of 2.01 eV corresponding to the transition energy at the **K** point.
- As the number of monolayers increases, the maximum value of DSP decreases to the bulk value of 70 % a 1.91 eV.
- The MoS₂ monolayer structures are potential materials to be used for spintronics applications.

Phosphorous and Phosphorene

Black Phosphorous (BP)

- Allotropic forms of phosphorous: black, violet, red, and white, in different cristalline structures. [Karttunen et al. Chem. Phys. **9** 2550, (2008), Brown et al. Acta Cristal. **19**, 684 (1965)].
- Most stable phases of BP: orthorrombic (semiconductor), rombhoedric (semimetal) and cubic (metal) [Liu et al. Chem. Soc. Reviews, **44** 2732 (2015)].
- The semiconductor BP belongs to the spatial group Cmca (# 64) and arrange in atomic monolayers.

Phosphorene

a) STEM image of bulk BP. Space group #64 mmm. [R. J. Wu, et al., Microscopy and Microanalysis **21**, 109 (2015)].

Schematic of top and side views of 2 ML phosphorene. Space group #53 mmm

Band structure of BP and phosphorene (a) BP (b) Phosphorene

Structural parameters

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Dielectric function of BP - comparison with experiment

[H. Asahina and A. Morita, J. Phys. C: Solid State Phys. **17**, 1839 (1984)]

Dielectric function of BP and phosphorene

• The dielectric function is anisotropic and depends on the kind of structure monolayer, bilayer and bulk BP. $42/48$

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Summary

- We have studied the linear optical response of black Phosphorous and phosphorene.
- We have calculated the electronic band structure and the imaginary part of the dielectric function of black Phosphorous and phosphorene.

Conclusion

- Both the Black Phosphorous and phosphorene present a highly anisotropic optical response.
- Overall, the respective linear optical response spectrum decreases as BP goes from the bulk to the one monolayer structure

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Summary

• We have studied the atomic ML structures of α -In₂Se₃, MoS₂, and phosphorene through the calculation of their lineal, non linear or spin injection response.

General conclusions

- In general, the linear and nonlinear optical response is sensitive to changes of atomic structure and thicknesses of atomic MLs.
- Atomic monolayers of MoS₂ can be used for spintronics applications. In particular, it is possible to tailor the degree of spin polarization as a function of ML thickness by incidence of circularly polarized light.

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Computing facilities

Acknowledgements: CONACyT - Mexico.

Cluster

- 3 Intel Xeon *sixteen-core* nodes of 4U (192 cores) of 64 bits and 3 Tb of RAM p/node.
- 36 Intel Xeon dual *six-core* nodes (432 cores) of 64 bits and 48 Gb of RAM p/node.

Gracias por su atención